

Search for CPT symmetry violation in neutral flavour meson oscillations

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Symmetries in physics

Role of symmetries:

- Simplify the description of phenomena,
- Relation between symmetries and conservation of laws (e.g. Noether theorem),
- Symmetry as a methodological indication,
- Symmetries constraining dynamical laws,
- Symmetry breaking e.g. chiral fields, origin of mass, flavour physics
- ...

It is only slightly overstating the case to say that physics is the study of symmetry

P.W. Anderson, Science, New Series, Vol.177,no.4047 (1972) 393-396

C, P and T operators

Discrete symmetries:

- Charge conjugation (particle \rightarrow antiparticle)

$$\hat{C}|\vec{r}, t, q \rangle = e^{i\alpha_1} |\vec{r}, t, -q \rangle$$

- Parity (spatial reflection)

$$\hat{P}|\vec{r}, t, q \rangle = e^{i\alpha_2} |-\vec{r}, t, q \rangle$$

- Time reversal

$$\hat{T}|\vec{r}, t, q \rangle = e^{i\alpha_3} | \vec{r}, -t, q \rangle$$

$\alpha_1, \alpha_2, \alpha_3$ are real phases.

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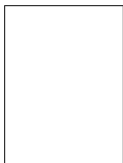
$\alpha_1, \alpha_2, \alpha_3$ are real phases.

All laws of physics seem to be unchanged under CPT transformation.

CPT theorem



Schwinger 1951



Lüdgers 1954



J S Bell 1954



Pauli 1955



Res Jost 1958

Taken for N. Mavromatos's talk: "Models and (some searches) for CPT violation"

CPT theorem (Schwinger, Bell, Jost, Pauli, Lunders)

A quantum field theory with the:

- hermitian,
- local Lagrangian,
- which conserves Lorentz symmetry
- and fulfils normal commutation(anti-commutation) rules

must have CPT symmetry (e.g. all particle theories in Standard Model (SM) but also many other proposed models).

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Phenomenological consequences: equality of particle/antiparticle masses, lifetimes, partial decay widths of mutually CPT-coupled channels etc.

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Remark (after J. Bernabeu): nothing in QM forbids CPT violation.

Experimental searches of CPT violation

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Precise tests of particle and antiparticle properties:

- positronium spectroscopy,
- experiments on beams of μ^+ , μ^- , $\pi^+\pi^-$ in vacuum,
- antihydrogen spectroscopy,
- search for electric dipole moments of neutrons, atoms, molecules,
- **mixing of neutral mesons.**

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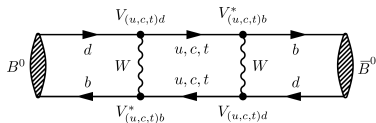
Interference effects in neutral flavour meson oscillation provide experimental precision reaching the Planck scale

e.g. $-4.0 \times 10^{-19} \text{ GeV} < m_{K^0} - m_{\bar{K}^0} < 4 \times 10^{-19} \text{ GeV}$ at 95 % C.L.

Particle Data Group 2015 - <http://pdg.lbl.gov/2015/reviews/rpp2015-rev-cpt-invariance-tests.pdf>

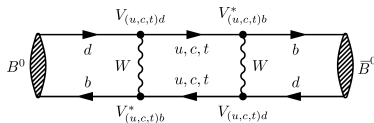
Oscillation phenomena

Weak interactions do not conserve the flavour



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Weak interactions do not conserve the flavour

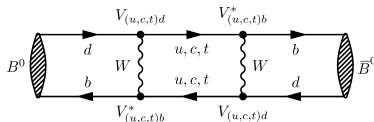


$|\rho^0\rangle, |\bar{\rho}^0\rangle$ are not eigenvectors of the full Hamiltonian

$$\frac{\partial}{\partial t}|\Phi\rangle = H|\Phi\rangle, \quad (1)$$

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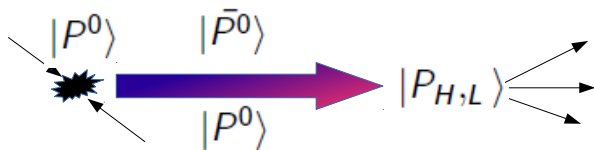
$$\frac{\partial}{\partial t} |\Phi\rangle = H |\Phi\rangle, \quad (1)$$

Mass eigenstates with given lifetimes (e.g. K_L, K_S) and not flavour eigenstates (e.g. K^0, \bar{K}^0)

$$\omega_{H,L} = m_{H,S} - \frac{i}{2} \Gamma_{H,L} \quad (2)$$

Oscillation phenomena

The neutral mesons oscillate back and forth in time between its particle and antiparticle states.



Weisskopf-Wigner approach

$$|\Phi\rangle = a(t)|P^0\rangle + b(t)|\bar{P}^0\rangle \quad (3)$$

$$\frac{\partial}{\partial t}|\Phi\rangle = H|\Phi\rangle, \quad (4)$$

- effective 2x2 Hamiltonian,
- time-independent,
- non-diagonal elements change flavour,
- non-Hermitian since decays outside of the $|P^0\rangle, |\bar{P}^0\rangle$ subspace,

$$H = M - \frac{i}{2}\Gamma, \quad (5)$$

M and Γ are hermitian matrices (mass and decay matrix, respectively).

CP parameterization

$$\begin{aligned} |P_L\rangle &= p|P^0\rangle + q|\bar{P}^0\rangle \\ |P_H\rangle &= p|P^0\rangle - q|\bar{P}^0\rangle, \end{aligned} \quad (6)$$

$$\frac{q^2}{p^2} = \frac{M_{12}^* - \frac{i}{2}\Gamma_{12}^*}{M_{12} - \frac{i}{2}\Gamma_{12}} \quad (7)$$

- Conservation of CP or T: $|\frac{q}{p}| = 1$

CPT parameterization

$$\begin{aligned} |P_L\rangle &= p\sqrt{1-z}|P^0\rangle + q\sqrt{1+z}|\bar{P}^0\rangle \\ |P_H\rangle &= p\sqrt{1+z}|P^0\rangle - q\sqrt{1-z}|\bar{P}^0\rangle, \end{aligned} \quad (8)$$

$$z = \frac{\delta m - \frac{i}{2}(\delta\Gamma)}{\Delta m - \frac{i}{2}\Delta\Gamma}, \quad (9)$$

where:

- $\delta m = M_{11} - M_{22}$ and $\delta\Gamma = \Gamma_{11} - \Gamma_{22}$,
- $\Delta m = m_H - m_L$ and $\Delta\Gamma = \Gamma_H - \Gamma_L$ (Δm and $\Delta\Gamma$ are generally very small !!!)

- Conservation of CP or CPT: $z = 0$
- Conservation of CP or T: $|\frac{q}{p}| = 1$

Oscillation phenomenology

Mixing parameters

$$\Delta m = m_H - m_L \text{ and } \Delta\Gamma = \Gamma_H - \Gamma_L,$$

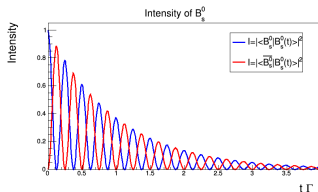
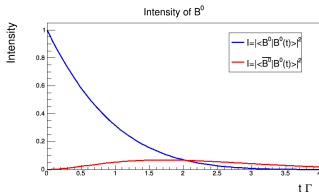
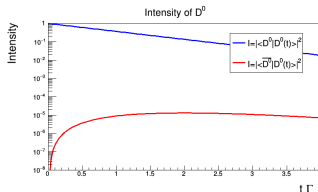
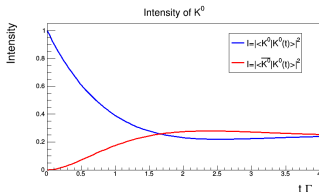
$$K^0 : x \approx 1, y \approx -1,$$

$$B^0 : x \approx 0.77, y \approx 0,$$

$$x = \frac{\Delta m}{\Gamma}, y = \frac{\Delta\Gamma}{2\Gamma}$$

$$D^0 : x \approx 0.001, y \approx 0.001,$$

$$B_s^0 : x \approx 26, y \approx 0.15,$$



Back to the 'ether' concept ? - Lorentz symmetry breaking

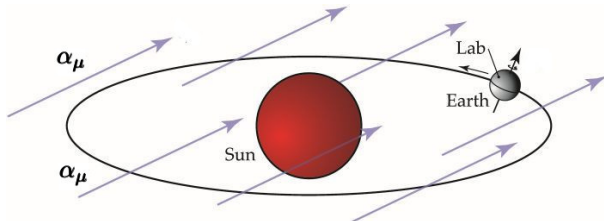
Greenberg theorem [PRL 89 (2002) 231602]

CPT violation implies Lorentz symmetry violation

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Greenberg theorem [PRL 89 (2002) 231602]

CPT violation implies Lorentz symmetry violation



The vacuum state is anisotropic in space which violates rotational invariance (Lorentz symmetry)

R. Lehnert Frascati Phys.Ser. 43 (2007) 131-154, MIT-CTP-3786 <http://arxiv.org/abs/hep-ph/0611177>

Lorentz symmetry violation introduces dependence of the particle boost and momentum direction.

Standard Model Extension(SME)

- Theoretical framework to test CPT violation in broad classes of experiments (Kostelecky, PRD55 (1997) 6760),
- Effective QFT with components breaking Lorentz and CPT symmetries,
- All properties of "good" QFT remain (renormalization, locality, spin-statistics relation, etc.);

$$z \simeq \frac{\beta^\mu \Delta a_\mu}{\Delta m - i\Delta\Gamma/2}, \quad (10)$$

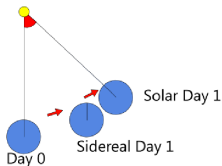
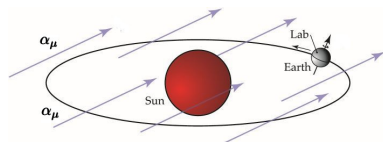
$\beta^\mu = \gamma(1, \vec{\beta})$ meson four-velocity in the observer frame

$$\Delta a_\mu \simeq a_\mu^{q1} - a_\mu^{q2}$$

a_μ valence quark coupling to Lorentz-violating field
(maybe expressed in some more fundamental physics beyond SME)

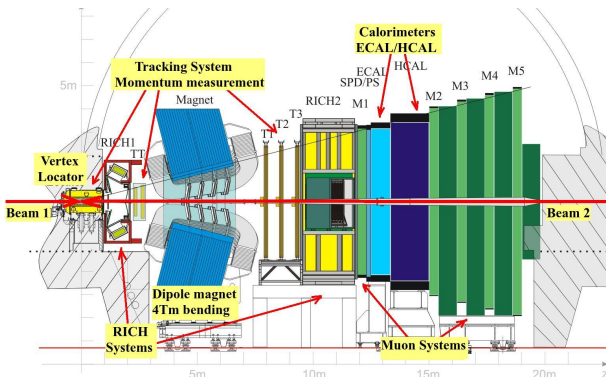
Sidereal modulations

CPT-violating observable z undergoes sidereal modulations, and depends on the geographical location of the detector.



- $\Phi_{sid} = \Omega \hat{t} = \Omega t_{GPS} + \Phi_{sid}^0$
- Sidereal angular frequency:
 $\Omega = \frac{2\pi}{T_{sid}} = 7.292 \times 10^{-11} \text{ rad } \mu\text{s}^{-1}$
- $T_{sol} = 86400\text{s}$
- $T_{sid} \approx \frac{365.25}{366.25} T_{sol} = 86164.1\text{s}$

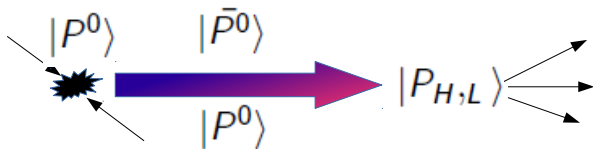
Large Hadron Collider beauty Detector



- Single-arm forward spectrometer covering range: $2 < \eta < 5$
($10 < \theta < 300$ (250) mrad)
- Momentum resolution: $\frac{\Delta p}{p} = 0.5\%$ at 5GeV/c to 1% at 200 GeV/c
- Impact parameter resolution: 20 μm for high p_T tracks

Experimental methodology in (heavy) neutral meson -recap

- 1 Determine (tag) initial flavour (P^0 or \bar{P}^0)
- 2 Determine (tag) final flavour (P^0 or \bar{P}^0)
- 3 From vertex displacement determine time
- 4 Construct time-dependent asymmetry ($A_{CPT}(t)$)
- 5 Fit the theoretical formula and extract CPT violating parameters ($\text{Re}(z)$, $\text{Im}(z)$)
- 6 in SME: search for the sidereal modulations, and direction dependence in $\text{Re}(z)$, and extract coupling parameters Δa_μ



Flavour-specific vs CP eigenstate

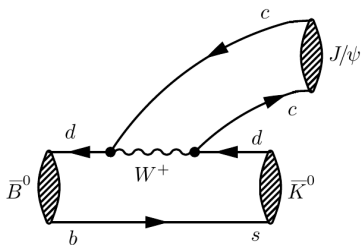
- decay to distinct flavour-specific state $A_{\bar{f}} = \bar{A}_f = 0$ e.g. in semi-leptonic decays (sensitive to $\text{Im}(z)$).
- decay to same CP final state $\bar{f} = f$ e.g. $B^0 \rightarrow J/\psi K_S^0$ (sensitive to $\text{Re}(z)$).

Time-dependent analyses in beauty sector

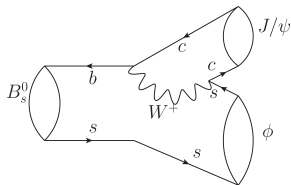
- Time-dependent analyses based on data gathered in 2011 and 2012 (3 fb^{-1} , pp @7 TeV and @8 TeV respectively).
- Both decays to CP final state (sensitivity to $\text{Re}(z)$, In SME: $|\frac{\text{Re}(z)}{\text{Im}(z)}| \gg 1$)

J. van Tilburg and M. van Veghel PLB 742 (2015) 236

- $B^0 \rightarrow J/\psi K_S^0$
- CP odd final state
- time-dependent fit

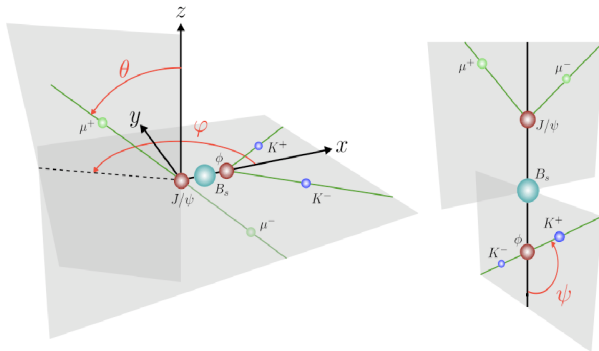


- $B_s^0 \rightarrow J/\psi \Phi$
- $P \rightarrow VV$
- $L = 0 \rightarrow L = 1$ and $L = 1$
- Mixture of CP odd and CP even final states
- time and angular dependent fit



Angular analysis of $B_s^0 \rightarrow J/\psi\phi$

The four polarization states can be separated statistically by measurement of three angles



$$\frac{d\Gamma}{d^3\vec{\Omega}dt} = \sum_{k=1}^{10} h_k(t) \times f_k(\vec{\Omega})$$

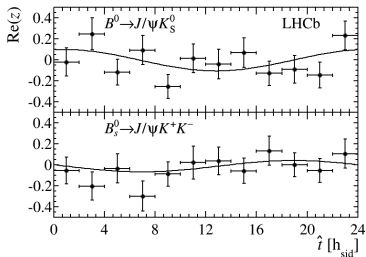
Results for $B^0 \rightarrow J/\psi K_S^0$ and $B_s^0 \rightarrow J/\psi \phi$

$$\text{Re}(z) = \frac{\gamma}{\Delta m} [\Delta a_0 + \beta \Delta a_Z \cos \chi + \beta \sin \chi (\Delta a_Y \sin \Omega \hat{t} + \Delta a_X \cos \Omega \hat{t})].$$

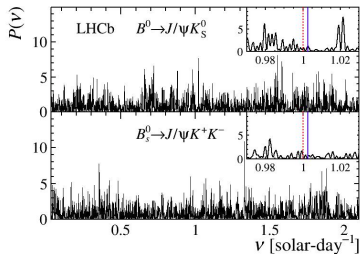
- Ω and \hat{t} - sidereal frequency and time respectively,
- Due to the LHCb geographical location: $\cos \chi = -0.38$ (const term), $\sin \chi = 0.92$ (sidereal modulated term)

PRL 116 (2016) 241601:

Re(z) as a function of sidereal phase



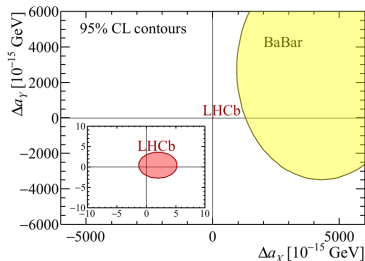
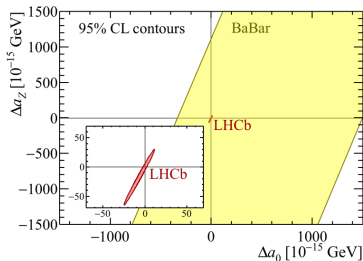
Periodogram analysis



Comparison with BaBar

LHCb - PRL 116 (2016) 241601: $B^0 \rightarrow J/\psi K_S^0$

$$\begin{aligned}\Delta a_0 - 0.38\Delta a_z &= -0.10 \pm 0.82 \pm 0.54 \times 10^{-15} \text{ GeV}, \\ 0.38\Delta a_0 + \Delta a_z &= -0.20 \pm 0.22 \pm 0.004 \times 10^{-13} \text{ GeV}, \\ \Delta a_x &= 1.97 \pm 1.30 \pm 0.29 \times 10^{-15} \text{ GeV}, \\ \Delta a_y &= 0.44 \pm 1.26 \pm 0.29 \times 10^{-15} \text{ GeV},\end{aligned}$$



- BaBar used inclusive dilepton B decays (PRL 100 (2008) 131801),
- Much smaller boost comparing to LHCb (0.5 vs 20),
- New LHCb result 1000 more precise than BaBar result.

Comparison with D0

LHCb - PRL 116 (2016) 241601: $B_s^0 \rightarrow J/\psi\Phi$

$$\Delta a_0 - 0.38\Delta a_z = -0.89 \pm 1.41 \pm 0.36 \times 10^{-14} \text{ GeV},$$

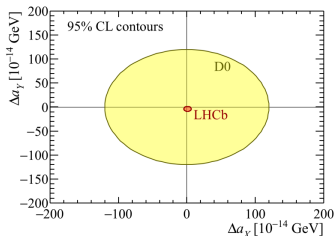
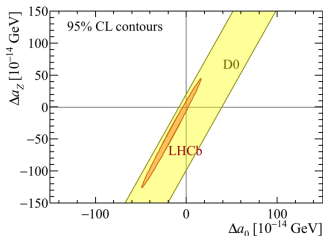
$$0.38\Delta a_0 + \Delta a_z = -0.47 \pm 0.22 \pm 0.08 \times 10^{-12} \text{ GeV},$$

$$\Delta a_x = 1.01 \pm 2.08 \pm 0.71 \times 10^{-14} \text{ GeV},$$

$$\Delta a_y = 3.83 \pm 2.09 \pm 0.71 \times 10^{-14} \text{ GeV},$$

$$\text{Re}z = -0.022 \pm 0.033 \pm 0.003 \text{ (Without assumption on Lorentz breaking)},$$

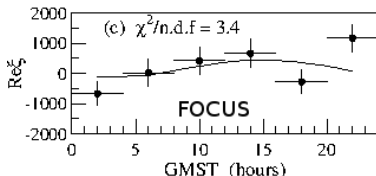
$$\text{Im}z = -0.004 \pm 0.011 \pm 0.002 \text{ (Without assumption on Lorentz breaking)}$$



- D0 used semileptonic B decays (PRL 115 (2015) 161601),
- Much smaller boost comparing to LHCb (4.7 vs 20),
- New LHCb result 10 more precise than D0 result.

Neutral charm sector

- Upper limit in the charm sector from FOCUS (PLB 556 (2003)7),
- Experiment @FERMILAB (γ beam with energy of ≈ 180 GeV on fixed BeO target),
- $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+$, both in classical and SME approach,
- $\text{Re}(z) - \text{Im}(z) \approx O(1)$,
- $\Delta a_\mu \approx 3 \times 10^{-13}$ GeV,

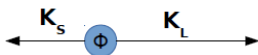


LHCb perspectives based on 2011 and 2012 data (3 fb^{-1}):

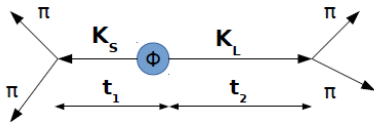
- Much higher statistics: $N_{LHCb} = 65 \times 10^6$ vs $N_{FOCUS} = 35 \times 10^3$,
- Similar boost
- Improvement by factor ≈ 44 (statistics).

Neutral strange sector - KLOE results

$$M(\Phi) = 1020 \text{ MeV}$$



Quantum entanglement (EPR)



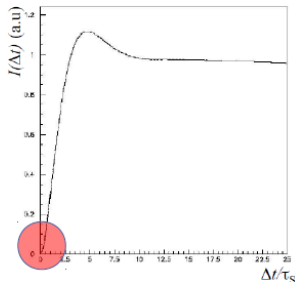
Quantum decoherence via gravity effects:

S. Hawking, Comm.Math.Phys.87 (1982) 395

$$\Phi \rightarrow K_S K_L$$

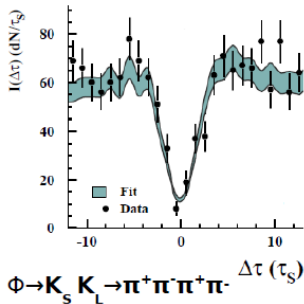
Antisymmetric quantum state

$$J^{PC} = 1^-$$



**Destructive interference
for identical final states**

Neutral strange sector - KLOE results



$$\Delta a_0 = (-6.0 \pm 7.7_{stat} \pm 3.1_{syst}) \times 10^{-18} \text{ GeV}$$

$$\Delta a_X = (0.9 \pm 1.5_{stat} \pm 0.6_{syst}) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Y = (-2.0 \pm 1.5_{stat} \pm 0.5_{syst}) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Z = (3.1 \pm 1.7_{stat} \pm 0.5_{syst}) \times 10^{-18} \text{ GeV}$$

D. Babusci et al. Phys. Lett. B 730C (2014), pp. 89-94

Summary

The LHCb provides new CPT limits in the beauty sector:

- The most precise limits for B^0 and B_s^0 provided,
- Classical limit for $\text{Re}(z)$ and $\text{Im}(z)$ in B_s^0 established for the first time.

- KLOE: $K^0 : \Delta a_0, \Delta a_{X,Y,Z} \approx 10^{-18}$ GeV
- FOCUS: $D^0 : \Delta a_0, \Delta a_{X,Y,Z} \approx 10^{-13}$ GeV
- LHCb: $B^0 : \Delta a_0, \Delta a_Z \approx 10^{-15}$ GeV, $\Delta a_X, \Delta a_Y \approx 10^{-15}$ GeV
- LHCb: $B_s^0 : \Delta a_0, \Delta a_Z \approx 10^{-12}$ GeV, $\Delta a_X, \Delta a_Y \approx 10^{-14}$ GeV

Outlook

- In the charm sector current limits can be improved with already collected LHCb data,
- In the beauty sector, by exploiting the decays to flavour-specific states, the improvement in $\text{Im}(z)$ is possible,
- New data from Run II:
 - expected data sample of about 5 fb^{-1} ,
 - energies from @7, @8 TeV to @13 TeV,
 - larger boost by a factor of 30 %.

THANK YOU FOR YOUR ATTENTION

BACKUP SLIDES

BACKUP SLIDES

Time evolution starting from a given flavour state

At $t = 0$:

$$|P^0\rangle = \frac{1}{2p}(\sqrt{1-z}|P_L\rangle + \sqrt{1+z}|P_H\rangle) \quad (12)$$

The time evolution will be given by:

$$|P^0(t)\rangle = \frac{1}{2p}(\sqrt{1-z}e^{-iM_L t}e^{-\Gamma_L t}|P_L\rangle + \sqrt{1+z}e^{-iM_H t}e^{-\Gamma_H t}|P_H\rangle) \quad (13)$$

which can be expressed again in $|P^0\rangle, |\bar{P}^0\rangle$ base:

$$|P^0(t)\rangle = g_+(t) + zg_-(t)|P^0\rangle - \frac{q}{p}\sqrt{1-z^2}g_-(t)|\bar{P}^0\rangle, \quad (14)$$

where: $g_{\pm}(t) = \frac{1}{2}(e^{-iM_H t}e^{-\Gamma_H t} \pm e^{-iM_L t}e^{-\Gamma_L t})$.

CP, T, CPT in z, ρ, q language

- Conservation of CP or CPT: $z = 0$
- Conservation of CP or T: $|\frac{q}{p}| = 1$

CPT is conserved when:

- 1 CP, and T is conserved ($z = 0, |\frac{q}{p}| = 1$)
- 2 no CP nor T are conserved ($z = 0, |\frac{q}{p}| \neq 1$)

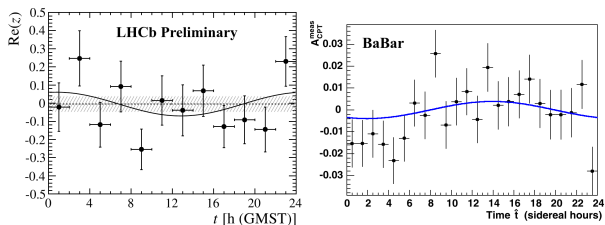
CPT is not conserved when:

- 1 CP is not conserved and T is conserved ($z \neq 0, |\frac{q}{p}| = 1$)
- 2 CP is conserved and T is not conserved ($z = 0, |\frac{q}{p}| \neq 1$)
- 3 no CP nor T are conserved ($z \neq 0, |\frac{q}{p}| \neq 1$)

One cannot experimentally distinguish between CPT conserved or violated if $z = 0, |\frac{q}{p}| = 1$.

Results for $B^0 \rightarrow J/\psi K_S^0$

LHCb (PRL 116 (2016) 241601)



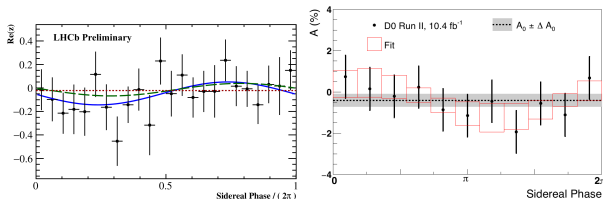
BaBar PRL 100, 131802 (2008)

$$\Delta a_0 - 0.30\Delta a_z = 0.6 \pm 0.5 \times 10^{-14} \text{ GeV},$$

$$\Delta a_x = 4.2 \pm 1.3 \times 10^{-14} \text{ GeV},$$

$$\Delta a_y = 2.6 \pm 2.5 \times 10^{-14} \text{ GeV},$$

Results for $B_s^0 \rightarrow J/\psi\phi$



D0: $B_s^0 \rightarrow \mu^\pm D_s^\mp$ PRL 115, 161601 (2015)

$a_{\text{perpend}} < 1.2 \times 10^{-12}$ GeV,

$-0.8 < \Delta a_0 - 0.396\Delta a_z < 3.9 \times 10^{-13}$ GeV,

CP, T and CPT symmetry

Conditions for H elements assuming CP/T/CPT symmetry:

$$[H, U] = 0 \leftrightarrow U^{-1}HU = H \quad (15)$$

- Conservation of CP or CPT:
 $H_{11} = H_{22} \rightarrow M_{11} = M_{22}, \Gamma_{11} = \Gamma_{22}$.
(Equality of masses and decay rates)
- Conservation of CP or T: $|H_{12}| = |H_{21}|$.

LHCb parameters

- LHC beam energy in pp collisions (\sqrt{s}): 7 and 8 TeV (2010-2012), 13 to 14 TeV (ongoing Run II)
- Collected integrated luminosity: 1 fb⁻¹ (2011), 2 fb⁻¹ (2012)
- Acceptance: 2 η ≤ 5
- data taking efficiency $\approx 90\%$
- trigger efficiency: 90 % for dimuon channels, 30% for multi-body hadronic final states
- track reco. efficiency: $\approx 96\%$ for long tracks
- Momentum resolution: $\frac{\Delta p}{p} = 0.5\%$ for low momentum till 1% at 200 GeV/c
- ECAL resolution: 1% + 10% $\sqrt{E[\text{GeV}]}$
- impact parameter resolution: 20 μm for high-pT tracks
- invariant mass resolution: 8 MeV/c² for B to J/Psi decays, 22 MeV/c² for two-body B decays, 100 MeV/c² for B to phi photon
- decay time resolution: 45 fs for Bs to J/Psi and Bs to Ds pi
- electron ID efficiency: 90 % (5 % miss probability)
- kaon ID efficiency: 95 % (5 % miss probability)
- muon ID efficiency: 97 % (1-3 % miss probability)